BUCKLING CURVES FOR HEAVY WIDE FLANGE STEEL **COLUMNS**

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Abstract: This paper proposes existing European buckling curves to be used for checking the resistance of heavy wide flange columns made from mild and highstrength steel, failing by flexural buckling. Buckling curves are not available in the current Eurocode3 EN 1993-1-1, for height-to-width ratios h/b > 1.2 and flange thicknesses $t_{\rm f} > 100$ mm. The buckling curves are evaluated according to the statistical procedure given in Annex D of EN 1990 using finite element analyses. Residual stress models as described in literature were used to define the initial stress state of the column in the finite element model. A large database was created containing the ratio between the elastic-plastic buckling resistance obtained from finite element analysis and the buckling resistance obtained from the proposed buckling curve for a wide set of column configurations from which a partial factor γ_{Rd} was deduced. Different section types with flange thicknesses $t_f > 100$ mm were investigated: the stocky HD and more slender HL type, featuring h/b = 1.23 and h/b = 1.232.35 respectively. The materials investigated were:

- Quenched and Self-Tempered (QST) steel available under the proprietary name HISTAR 460 (High Strength ArcelorMittal) with a yield stress of 460 N/mm²;
- steel grade S460;
- steel grade S355;
- steel grade S235.

For as far as available, statistical information on these materials was used to estimate the partial factor for material properties γ_{m} . Then the partial (safety) factor γ_{M1} can be calculated as $\gamma_{M1} = \gamma_{Rd} \cdot \gamma_{m}$. Based on the criterion that γ_{M1} should not exceed 1.05, buckling curves are suggested which can be used together with γ_{M1} = 1.0. Buckling curves to be included in Eurocode3 EN 1993-1-1 are finally proposed for heavy wide flange columns in S235 to S500, with cross-sections with height-to-width ratios h/b>1.2 and flange thicknesses $t_f > 100$ mm.

This paper is an extended and more complete version of an earlier paper [1].

Keywords: Buckling curves, Finite element analyses, Heavy wide flange sections, High-strength steel, Mild steel, Partial factor, Statistical evaluation.

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1. INTRODUCTION

The advent of Quenched and Self-Tempered (QST) steel sections which combine high strength (i.e. nominal yield stress greater than 430 N/mm²) with good ductility and weldability has led to a broadening of the possibilities in steel construction. This manufacturing method can also be applied to produce heavy wide flange sections, i.e. wide flange sections with flanges thicker than 40 mm. At the moment, heavy wide flange QST sections are manufactured by ArcelorMittal under the proprietary name of HISTAR (HIgh-STrength ARcelorMittal). Two grades are currently produced: HISTAR 355 and (high-strength) HISTAR 460, which possess a yield stress of 355 N/mm² and 460 N/mm² respectively, not considering reduction of yield stress with increasing material thickness. Heavy wide flange HISTAR 460 sections have already been applied worldwide, with the majority in the United States where the US equivalent of HISTAR 460, Grade 65, is covered by ASTM A913 [2, 3].

Besides the high yield stress, HISTAR 460 sections have improved material properties for wide flange sections possessing thick flanges. For HISTAR 460 a smaller reduction in yield stress needs to be incorporated for greater material thicknesses according to ETA-10/0156 [4] when compared to other grades (e.g. S460M and S500M according to EN 10025-4 [5]) as illustrated in Figure 1. For HISTAR 460 and S460 sections with flange thicknesses exceeding 100 mm, the yield stress is 450 and 385 N/mm² respectively.

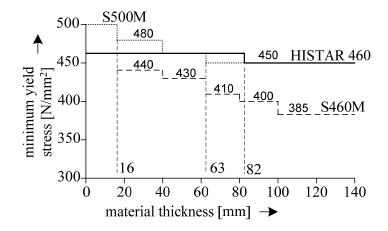


Fig. 1 - Decrease of yield stress of HISTAR 460, S460 and S500 with increasing material thickness

For S355 and S235, depending on whether the material is classified as a non-alloy structural steel, normalized fine grain structural steel or thermomechanical fine grain steel according to EN 10025-2 [6], EN 10025-3 [7] and EN 10025-4 [5],

respectively, a substantially reduced yield stress must be used to account for a reduction in material properties for thick plated parts. For the present study with sections possessing flange thicknesses between 100 and 150 mm, the yield stress for S235 steel is 195 N/mm². For S355 the lowest yield stress value according to the three different standards is selected: 295 N/mm².

As such, heavy wide flange HISTAR 460 sections are used to their best advantage when the ultimate limit state is the governing design criterion. This is the case when applied as gravity columns in multi-story buildings, beams in short-or medium-span bridges or chord- and brace members as part of truss-like structures. In these situations the design is most often controlled by the flexural buckling resistance of the member for which due allowance has to be made according to the relevant design codes.

				Buckling	curve
			Buckling	S 235	S460
Cross-section		Limits	about	S 275	
			axis	S 355	
				S 420	
Rolled I-sections		$t_{\rm f} \le 40~{\rm mm}$	у-у	a	a_0
Z	h/b > 1.2	$t_{\rm f} \ge 40~{\rm Hill}$	z-z	b	a_0
	n/0 > 1.2				
t_{f}		$40 < t_{\rm f} \le 100 \text{mm}$	у-у	b	a
		$40 < t_{\rm f} \le 100 \text{ mm}$	z-z	c	a
${y}$ h			у-у	b	a
	$h/b \le 1.2$ $t_{\rm f} \le 100 {\rm mm}$		Z-Z	c	a
			_		
$\downarrow z$ $\downarrow b$		$t_{\rm f} > 100 \; {\rm mm}$	y-y z-z	d d	c c

Table 1 - Buckling curve selection table according to Eurocode3, EN 1993-1-1

HISTAR 460 falls in the category S460 in Table 1. Small and medium-sized HISTAR 460 sections with flange thickness $t_{\rm f}$ smaller than or equal to 40 mm are assigned to buckling curve "a" or "a₀" depending on the value of the height-to-width ratio h/b. Heavy HISTAR 460 sections which have a flange thickness smaller than or equal to 100 mm can be designed according to buckling curve "a". Heavy sections possessing a flange thickness in excess of 100 mm and an h/b-ratio smaller than 1.2 are assigned to buckling curve "c". For heavy HISTAR 460 sections having h/b-ratios greater than 1.2 and flanges thicker than 100 mm no buckling curves are available. The same is true for heavy sections in S460, S355 and S235 for h/b > 1.2 and $t_{\rm f} > 100$ mm.

In order to arrive at buckling curves reflecting the buckling response for heavy sections in HISTAR 460, S460, S355 and S235 with flange thickness larger than 100 mm and h/b-ratios greater than 1.2, a combined experimental and numerical study was initiated by ArcelorMittal in Luxemburg and set up and executed by Eindhoven University of Technology in the Netherlands. The experiments consisted of residual stress measurements performed on two different heavy wide flange section types made in steel grade HISTAR 460. A residual stress model was proposed which can be used for heavy wide flange OST sections. The testing procedure and the derivation of this so called 'QST residual stress model' are detailed in [9]. Since the manufacturing process of heavy \$460 sections is identical to that of HISTAR 460 sections, the residual stress model of the latter was applied to the S460 analyses. As no experimental data is available to model the residual stresses state for heavy HL sections made from S235 or S355 an assumption was made on their distribution. For the S235 members the so called 'ECCS residual stress model' [10] featuring a bilinear stress pattern over the web height and flange width was used to define the initial stress state. For the sections made from S355 steel the QST residual stress model was adopted in addition to the ECCS residual stress model.

In the present paper, existing ECCS buckling curves are proposed to check the flexural buckling resistance of heavy HISTAR 460 sections. The reliability of the suggested buckling curves is evaluated according to annex D of EN 1990 [11]. The buckling resistance for a wide set of columns in HISTAR 460, S460, S355 and S235 is evaluated with the finite element method using the residual stress models mentioned to define the initial stress state of the column and with widely accepted geometric imperfections.

1.1 Earlier approaches for derivation of buckling curves

From the earliest experiments on pin-ended columns failing by flexural buckling it was observed that the slenderness (ratio between length and radius of gyration) of the member has profound influence on the buckling response. This led to the development of the buckling curve concept, relating the load a column can withstand before instability occurs to its non-dimensional or relative slenderness (slenderness normalized against the steel properties). Important references include [12, 13]. The studies underlying the buckling curve concept were often based on a two-fold approach: to obtain the elastic-plastic buckling resistance through full-scale column testing and to conduct theoretical (and later numerical) analyses to replicate and supplement the experimental results. The theoretical analyses were expanded to include a wide set of columns not part of the experimental plan from which design rules (buckling curves) were proposed. The accuracy of the buckling curve was often evaluated through comparison with characteristic values from full-

scale tests performed, where 'good agreement' between the buckling curve and test justified the selected buckling curve.

1.2 Statistical evaluation of resistance models

The earlier approaches to arrive at buckling curve formulations have become obsolete as with the appearance of EN 1990 Annex D [11] "Design assisted by testing" it is now possible to make a statistical evaluation for new design rules and existing ones and to quantify the variability of salient parameters. In brief, the EN-1990 states that the design resistance (R_d) may be obtained directly from the quotient of the characteristic (R_k) strength and the partial factor γ_M :

$$R_{\rm d} = \frac{R_{\rm k}}{\gamma_{\rm M}} \tag{1}$$

Where $\gamma_{\rm M}$ can be subdivided as follows:

$$\gamma_{\rm M} = \gamma_{\rm Rd} \cdot \gamma_{\rm m} \tag{2}$$

Where:

 γ_{M} is the partial factor for a material property, also accounting for model uncertainties and dimensional variations according to EN 1990 [11] or general partial factor according to EN 1993-1-1 [8];

 γ_{Rd} is the partial factor associated with the uncertainty of the resistance model;

 $\gamma_{\rm m}$ is the partial factor for a material property.

A distinction for the general partial factor $\gamma_{\rm M}$ is made depending on the failure mode of the member under investigation. In the present study, columns are investigated for which loss of stability is the governing failure mode. Therefore the general partial factor is – in line with EN 1993-1-1 - denoted γMI throughout this paper. The general partial factor serves as a reduction for the section capacity: high $\gamma_{\rm MI}$ -values impose a larger reduction on the buckling capacity compared to lower $\gamma_{\rm MI}$ -values.

One of the earliest studies concerning the statistical evaluation of resistance models was carried out by Sedlacek et al. [14] at RWTH Aachen, Germany. Although the investigation was performed prior to the final appearance of EN 1990, it adopted the same methodology. The study was aimed at finding new imperfection factors for the resistance model of Eurocode3 (EN 1993-1-1) to check the lateral-torsional buckling resistance of rolled and welded beams. The reliability of the old resistance model, originally from the DIN, in addition to the new

resistance model was re-evaluated. The statistical evaluation was based on 144 lateral-torsional buckling tests.

A probabilistic assessment of the existing design rules to check the lateral torsional buckling resistance of beams was performed by the University of Coimbra, Portugal for wide flange beams. The partial factor associated with the uncertainty of the resistance model γ_{Rd} was computed for different load cases and section types using the three different design models for lateral torsional buckling available in EN 1993-1-1, Rebelo et al. [15]. The evaluation of the partial factors was based on the solution results from finite element analyses conducted on a wide set of beam configurations.

In the accompanying paper by Simoes da Silva et al. [16], the partial factor for the material properties γ_m was determined based on tensile tests conducted on sections made from different steel grades. Using equation (2), the factors from [15, 16] were used to arrive at γ_{M1} -values for different load cases and steel grades.

1.3 Present Study

In the present study the methodology adopted by Rebelo et al. [15] and in line with Annex D of EN 1990 will be used to check the reliability of proposed buckling curves for heavy wide flange sections.

A large database is created containing the ratio between the elastic-plastic buckling resistance obtained from non-linear finite element analyses and buckling resistances obtained from the suggested buckling curve for a wide set of column configurations. It is mentioned that the numerically obtained elastic-plastic buckling resistance serves as a replacement of the ultimate resistance found in a column buckling test. The ratio between both buckling resistances for a specific set of columns is used to compute the partial factor γ_{Rd} associated with the uncertainty of the resistance model.

For S460, statistical literature information concerning the relevant material property, being the yield stress f_y , is used to estimate $\gamma_m < 1.0$. Then the general partial factor γ_{M1} is computed according to equation (2). Since for HISTAR 460 such information is not yet available $\gamma_m = 1.0$ can be conservatively used to compute the general partial factor γ_{M1} according to equation (2). This general partial factor can have a lower value in the nearby future pending the availability of a lower γ_m -value representing the variability in mechanical properties of HISTAR 460 steels. For S355 and S235 $\gamma_m = 1.0$ was also conservatively adopted to compute the general partial factor γ_{M1} according to equation (2).

The study is limited to heavy wide flange sections which possess a flange thickness (t_f) greater than 100 mm and for which the height-to-width ratio (h/b) is greater than 1.2. The selected sections for the present study are listed in Table 2. In the present study a distinction is made between HD en HL sections, having an h/b-value of approximately 1.23 and 2.35, respectively.

•	•	•			-	
Section name: European American – Imperial	Weight per m [kg]	h [mm]	b [mm]	t _w [mm]	t _f [mm]	h/b [-]
HD 400 x 900 W14x16x605	900	531	442	65.9	106	1.20
HD 400 x 990 W14x16x665	990	550	448	71.9	115	1.23
HD 400 x 1086 W14x16x730	1086	569	454	78	125	1.25
HD 400 x 1202 W14x16x808	1202	580	471	95	130	1.23
HD 400 x 1299 W14x16x873	1299	600	476	100	140	1.26
HL 920 x 1194 W36x16.5x802	1194	1081	457	60.5	109	2.37
HL 920 x 1269 W36x16.5x853	1269	1093	461	64	115.1	2.37
HL 920 x 1377 W36x16 5x925	1377	1093	473	76.7	115.1	2.31

Table 2 - Heavy wide flange sections offered by ArcelorMittal with h/b > 1.2 and $t_f > 100$ mm

2. BUCKLING CURVE FORMULATION

The theoretical resistance defining the maximum compressive force a column can withstand before failing in a flexural buckling mode is determined using EN 1993-1-1 [8]. The buckling resistance for a column can be verified as follows:

$$\frac{N_{\rm Ed}}{N_{\rm b,Rd}} \le 1.0 \tag{3}$$

Where:

 $N_{\rm E,d}$ is the design value of the compression force;

 $N_{\rm b,Rd}$ is the design buckling resistance.

The design buckling resistance is given by:

$$N_{b,Rd} = \frac{\chi A f_{y}}{\gamma_{M1}} \tag{4}$$

Where A is the cross-sectional area, f_y is the yield stress, γ_{M1} is the general partial factor for instability and χ is the buckling reduction factor. This check is only valid for sections belonging to cross-sectional class 1, 2 or 3. The product of the cross-sectional area and the yield stress is known as the squash load of the cross-section or N_{pl} . Using equations (3, 4), the verification of the buckling resistance can be rewritten as follows:

$$\frac{N_{\rm Ed}}{\chi N_{\rm pl}/\gamma_{\rm Ml}} \le 1.0 \tag{5}$$

The buckling reduction factor can be computed according to:

$$\chi = \frac{1}{\Phi + \sqrt{\Phi^2 - \overline{\lambda}^2}} \text{ but } \chi \le 1.0$$
 (6)

Where:

$$\Phi = 0.5 \left(1 + \alpha \left(\overline{\lambda} - 0.2 \right) + \overline{\lambda}^2 \right) \tag{7}$$

The relative slenderness $\overline{\lambda}$ can be determined as follows:

$$\overline{\lambda} = \sqrt{N_{\rm pl}/N_{\rm cr}} \tag{8}$$

Where $N_{\rm cr}$ is the elastic critical force of the column. The imperfection factor α attains one of the values as listed in Table 3, depending on the cross-section, steel grade and buckling case (weak-axis or strong-axis buckling) under consideration.

Table 3 - Imperfection factor for buckling curves

Buckling curve	a_0	a	b	С	d
Imperfection factor α	0.13	0.21	0.34	0.49	0.76

A graphical representation of the buckling curves is shown in Figure 2. Based on the selected buckling curve and corresponding imperfection factor a theoretical resistance χ can be computed for a heavy section if the relative slenderness is known. This value will be compared to the elastic-plastic buckling resistance obtained from non-linear finite element analysis (Section 3).

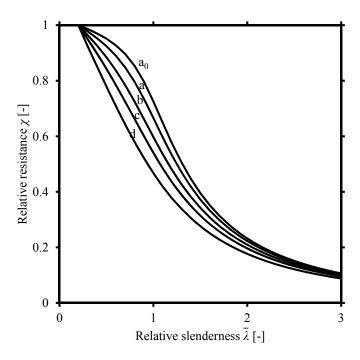


Fig. 2 - Buckling curves from Eurocode3

3. FINITE ELEMENT MODEL

3.1 Elements

The geometrical and material non-linear analyses on the columns containing imperfections (GMNIA) were performed in the ANSYS v.11.0 implicit environment. The columns were modelled with beam elements. The 3D three node finite strain element (BEAM189) was selected for the analyses as it can describe plasticity, large deformations and large strains. A user-defined cross-section was modelled based on nominal dimensions, see Table 2. The cross-section is subdivided into different cells to capture growth of plastic zones across the cross-section. Each cell contains four integration points where the stresses are evaluated (Figure 4a). Two integration point locations in longitudinal direction of each element describe progressive yielding along the length of the column. A total of 20 elements along the length of the member were considered sufficient. Earlier research studies on column buckling have shown that this element type is able to replicate experimental elastic-plastic buckling tests with good accuracy thereby taking into account the effects of residual stresses [17, 18].

3.2 Boundary conditions

All selected column configurations for the present investigations were simply supported. The column was pin-supported and torsionally restrained at the bottom. The same boundary condition was applied at the top with the exception that vertical translation was permitted. For the evaluation of strong-axis buckling, the column was restrained against weak-axis deflections by translational supports along the length (Figure 3).

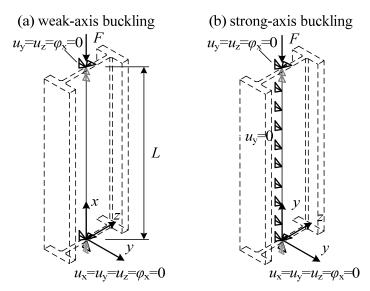


Fig. 3 - Boundary conditions

3.3 Residual stresses

An individual residual stress value was set for each integration point in the cross-section. The stress value specified for each integration point is assigned to the tributary area belonging to that integration point, rendering a step-wise initial stress pattern over the cross-section (Figure 4b). Here the pattern for the residual stress model of [9] for HISTAR 460 is shown. The residual stresses are constant across the flange thickness and web thickness. After inserting the residual stresses into the element, a first solution step was issued to verify internal equilibrium of the residual stress model. Insignificant differences were observed between the residual stress model and the stresses after solving, indicating correct implementation of the residual stress model (Figure 4c).

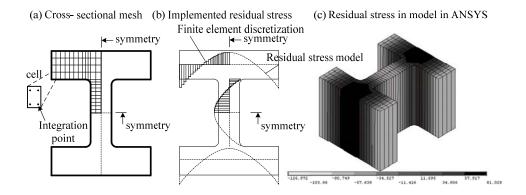


Fig. 4 - Finite element discretization of cross-section and implemented residual stresses (for HD 400x1202)

For HISTAR 460 and for S460, the QST residual stress model of [9] was adopted as depicted in (Figure 5a). This model has a parabolic shape along the web height and flange width. The magnitude of the residual stresses in the web is related to the section dimensions.

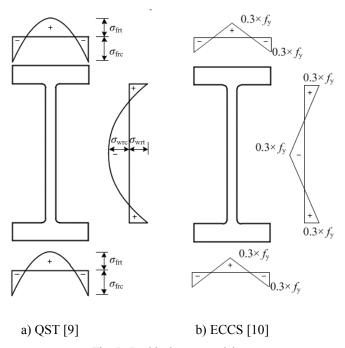


Fig. 5 - Residual stress models

Currently no experimental data on the residual stress distribution in mild steel HL and HD sections is known to the authors. In order to include the effect of residual stress on the resistance of these sections when failing by strong- and weakaxis buckling an assumption is made about their distribution. Two different residual models are selected to make an educated guess concerning the residual stresses: the ECCS residual stress model [10] commonly used for wide flange hotrolled sections (Figure 5b) and the earlier derived QST residual stress model (Figure 5a). As the latter model has residual stress values exceeding the (reduced) yield stress of S235 steels, which is physically not possible, the QST residual stress model is not used for the S235 columns. The ECCS residual stress model is featured by a bi-linear stress distribution along the web height and flange widths. The extreme values are at the flange tips and web center (compression) and webto-flange junction (tension) and set at 30 % of the (unreduced) yield stress. The unreduced yield stresses, $f_v = 235 \text{ N/mm}^2$ and $f_y = 355 \text{ N/mm}^2$ for S235 and S355 respectively, were used which is conservative in view of defining the residual stress values. Using $f_y = 355 \text{ N/mm}^2$ may be very conservative since normally $f_y =$ 235 N/mm² is used with the ECCS residual stress model regardless the steel grade.

The residual stress values at the most critical locations for the QST and ECCS residual stress models are listed in Table 4 and Table 5, respectively.

Steel grade	Section	$\sigma_{ m frt}$ (tension)	$\sigma_{ m frc}$ (compression)	$\sigma_{ m wrt}$ (tension)	$\sigma_{ m wrc}$ (compression)
	HD 400 x 900	81	135	81	101
HISTAR460	HD 400 x 990	81	135	81	101
	HD 400 x 1086	81	135	81	102
S460	HD 400 x 1202	81	135	81	95
	HD 400 x 1299	81	135	81	97
S355	HL 920 x 1194	180	225	180	219
	HL 920 x 1269	180	225	180	220
	HL 920 x 1377	180	225	180	201

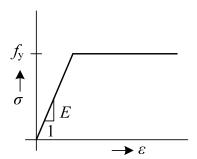
Table 4 - Residual stress values for QST residual stress model [9] [N/mm2]

Table 5 - Residual stress values for ECCS residual stress model [10] [N/mm2]

Steel grade	Section	Flange tip/web center (compression)	Web-to-flange junction (tension)
S235	all	$0.3 \cdot 235 = 71$	$0.3 \cdot 235 = 71$
S355	all	$0.3 \cdot 355 = 107$	$0.3 \cdot 355 = 107$

3.4 Material model

A bi-linear material model was applied to describe the material's response to loading (Figure 6). A fixed yield stress value f_y was used to define the onset of yielding. This value is based on the steel properties, thereby taking into account a reduction in yield stress due to the thickness of the flanges. A more generally accepted value for the Young's modulus of 200 000 N/mm² was adopted to define the elastic stage of the material. Strain hardening increases the ultimate load of stocky columns but hardly affects columns in the intermediate and high slenderness ranges. Neglecting strain hardening is a conservative approach and is in line with what has previously been done by other researchers, e.g. [15, 16]. Therefore, no strain hardening effects were included.



Steel grade	Yield stress f_y [N/mm ²]				
HISTAR 460	450				
S460	385				
S355	295				
S235	195				
$E = 200000 \text{ N/mm}^2$					

Fig. 6 - Material model

3.5 Geometric imperfections

The shape of the geometric imperfection was based on the buckling mode belonging to the lowest eigenvalue from a linear buckling analysis. This resulted in a sinusoidal bow imperfection. The amplitude defining the maximum deviation from the ideal geometry was L/1000, where L is the height of the column. This approach is generally accepted for the determination of buckling curves. A similar approach, but then for lateral torsional buckling of beams, was used in [15]. The value L/1000 for the imperfection amplitude is recommended in [10]. This value is expected to be conservative since it is very likely that the real imperfections of the heavy sections considered here are smaller than L/1000. The value L/1000 is a design imperfection amplitude for use in numerical analyses.

3.6 Solution

All elastic-plastic buckling GMNIA are load-controlled. A force with specified magnitude was applied at the top of the column. The Arc-Length method

was selected to solve the non-linear equilibrium iterations. The Arc-Length method was selected in preference to the conventional Newton-Raphson method as the former is able to describe the decreasing load-deflection curve beyond the maximum load whereas the latter will abort the solution when the maximum resistance has been reached. The load was divided into four load steps which in turn were further divided into substeps or load increments. For each load-increment a number of equilibrium iterations were performed to arrive at a converged solution. The solution was considered solved when the out-of-balance load vector is smaller than 0.05 % of the load increment. The ultimate strength or flexural buckling resistance of the column ($N_{\rm ult;FEM}$) was identified as the maximum load on the load-deflection curve. The elastic buckling load ($N_{\rm cr;FEM}$) is obtained from a linear buckling analysis (LBA) using the Block-Lanczos extraction method of eigenvalues.

3.7 Plotting results in buckling curve

For each column configuration for which the ultimate resistance is evaluated through non-linear finite element analyses, the reduction factor is obtained by normalizing the ultimate load against the squash load of the cross-section ($N_{\rm pl;FEM}$).

$$\chi_{\text{FEM}} = \frac{N_{\text{ult;FEM}}}{N_{\text{pl;FEM}}} \tag{9}$$

Where the squash load of the cross-section is computed according to:

$$N_{\rm pl;FEM} = Af_{\rm y} \tag{10}$$

Where A is the cross-sectional area of the element and f_y is the yield stress.

The factor χ_{FEM} is labeled as the 'experimental' resistance for comparison with the theoretical resistance χ . The relative slenderness of the column can be computed by taking the square root of the ratio between the squash load of the cross-section and the elastic buckling load evaluated from a linear buckling analysis:

$$\overline{\lambda}_{\text{FEM}} = \sqrt{N_{\text{pl;FEM}}/N_{\text{cr;FEM}}}$$
 (11)

Note that equation (11) is similar to equation (8) but the squash load is now based on that of the FEM model and the elastic buckling load is calculated with a LBA.

3.8 Finite element results

3.8.1 Steel HISTAR 460

Typical load-deflection curves as obtained from the finite element analyses are shown in Figure 7a.

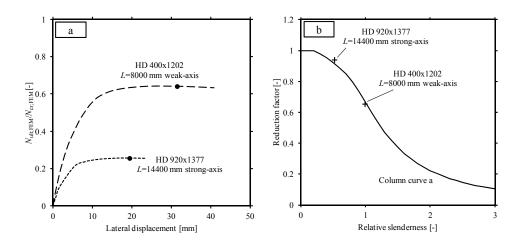


Fig. 7 - Finite element output: load-deflection curves for HISTAR 460 (a) and corresponding data in buckling curve diagram (b)

In Figure 7b the ultimate loads from Figure 7a are plotted in the buckling curve diagram using the equations (10, 11) in addition to buckling curve "a". Plotting the ultimate load for a specific group of columns in the buckling curve diagram in addition to a buckling curve allows a first estimate to be made as to whether that specific buckling curve is on the conservative or unconservative side.

3.8.2 Steel grade S460

Typical load-deflection curves as obtained from finite element analyses are shown in Figure 8 for four HD 400x1299 columns in S460 failing by weak-axis buckling.

In Figure 9 the ultimate loads from Figure 8 are plotted in the buckling curve diagram using the equations (10, 11) in addition to buckling curve "b" to show that there is a reasonable fit with buckling curve "b" slightly on the conservative side.

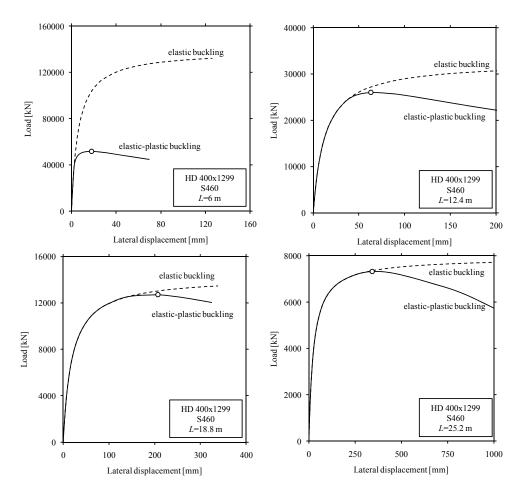


Fig. 8 - Finite element output: load-deflection curves for elastic and elastic-plastic buckling analyses of HD 400x1299 columns in S460

3.8.3 Steel grades S355 and S235

Typical load-deflection curves for strong axis buckling as obtained from finite element analyses are shown in Figure 10 for columns with different lengths with cross-section HL 920x1377 in S355 and S235 using the QST and ECCS residual stress models.

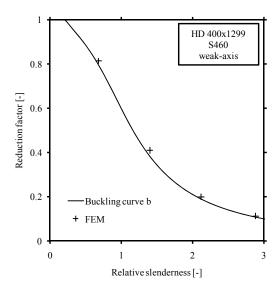


Fig. 9 - Finite element results plotted in buckling curve diagram for buckling of HD 400x1299 columns in S460

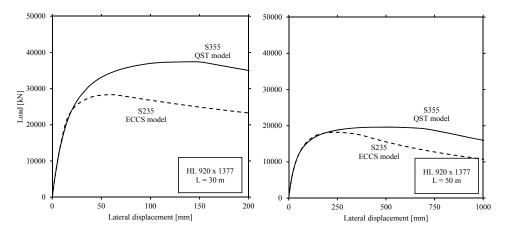


Fig. 10 - Finite element output: load-deflection curves for buckling analyses of HL 920x1377 columns

In Figure 11 the ultimate loads from Figure 10 are plotted in the buckling curve diagram using the equations (10, 11) in addition to buckling curve "a" to show that there is a reasonable fit.

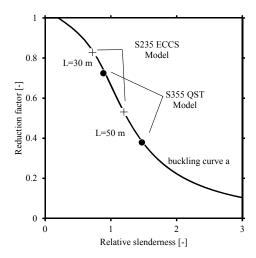


Fig. 11 - Finite element results plotted in buckling curve diagram for buckling of HL 920x1377 columns

4. STATISTICAL EVALUATION AND SUGGESTED BUCKLING CURVES

4.1 Partial factor evaluation procedure

The partial factor evaluation procedure follows Annex D of EN 1990 and is applied here in a similar way as in [15]. For any heavy QST column i a comparison can be made between its experimental resistance $(r_{e,i})$ and its theoretical resistance $(r_{t,i})$:

$$R_{\rm i} = \frac{r_{\rm e,i}}{r_{\rm t,i}} \tag{12}$$

In the present study the experimental resistance refers to χ_{FEM} from equation (9) for a column i failing by flexural buckling as obtained from non-linear finite element analysis, so $r_{\text{e,i}} = \chi_{\text{FEM}}$. The theoretical resistance of column i refers to the buckling reduction factor χ according to the buckling curve formulation from EN 1993-1-1 (equation (6)), so $r_{\text{t,i}} = \chi$. It is noted that in order to arrive at a theoretical resistance a selection for a buckling curve (imperfection factor from Table 3) must already be made. A value of R_i smaller than 1.0 or larger than 1.0 reflects an unconservative or a conservative theoretical resistance model, respectively. For any group of column configurations belonging to a set with sample size n, the mean value correction factor R_m and corresponding variance can be determined:

$$R_{\rm m} = \frac{1}{n} \sum_{i=1}^{n} R_{\rm i} \quad \sigma_{\rm R}^2 = \frac{1}{n-1} \sum_{i=1}^{n} (R_{\rm i} - R_{\rm m})^2$$
 (13)

When plotting the experimental resistance on the y-axis and corresponding theoretical resistance on the x-axis for all column configurations belonging to subset n, the points will be distributed around the so-called estimator line: $r_e = R_m \cdot r_t$.

For each column configuration belonging to subset n an error term δ_i is introduced:

$$\delta_{\rm i} = \frac{r_{\rm e,i}}{r_{\rm t,i} \cdot R_{\rm m}} \tag{14}$$

A logarithmic transformation is performed:

$$\Delta_{i} = \ln(\delta_{i}) \tag{15}$$

For the logarithmic error terms belonging to sample size n, the mean value and corresponding variance are determined as follows:

$$\overline{\Delta} = \frac{1}{n} \sum_{i=1}^{n} \Delta_{i} \quad \sigma_{\Delta}^{2} = \frac{1}{n-1} \sum_{i=1}^{n} \left(\Delta_{i} - \overline{\Delta} \right)^{2}$$
 (16)

The variance can be used to compute the coefficient of variation as follows:

$$V_{\delta} = \sqrt{\exp(\sigma_{\Delta}^2) - 1} \tag{17}$$

When using a subset with a sample size n > 100 the partial factor associated with the uncertainty of the resistance model can be determined as follows:

$$\gamma_{\rm Rd} = \frac{1}{R_{\rm m} \exp\left(-k_{\rm d,n} Q - 0.5 Q^2\right)} \ge 1.0 \tag{18}$$

For which:

$$Q = \sqrt{\ln\left(V_{\delta}^2 + 1\right)} \tag{19}$$

And where $k_{\rm d,n}$ is the characteristic fractile factor: $0.8 \cdot 3.8 = 3.04$.

So, finally equation (18) gives the partial factor γ_{Rd} belonging to a suggested buckling curve based on a set of column configurations.

4.2 Partial factor for suggested buckling curves

Non-linear finite element analyses were carried out for the heavy wide flange cross-sections of Table 2. Per steel grade, cross-section, buckling axis and where appropriate residual stress model at least 100 analyses were performed indicated by the sample size n.

4.2.1 Steel HISTAR 460

For HISTAR 460 all eight cross-sections were considered, see Table 2. For each cross-section the weak-axis and strong-axis buckling response was evaluated. The relative slenderness of the investigated columns was in the range between 0.31 and 3.3.

Plotting the finite element results in a buckling curve diagram permits a first judgment on the suitability of the buckling curve to represent the column strength for heavy HISTAR 460 sections. In case the chosen buckling curve is positioned below the finite element results, it will provide conservative column strength values. The buckling curve can be regarded as unconservative when the finite element data is below the buckling curve. Figure 12 (left) shows the finite elements results for a HL 400x1202 section in HISTAR 460 buckling about its weak axis in a buckling curve diagram in addition to buckling curve "b".

Similar trends are found when plotting the theoretical column strength $r_{t,i} = \chi$ against its numerical counterpart $r_{e,i} = \chi_{FEM}$ such as shown in Figure 12 (right). In case the buckling curve produces column strengths similar to the finite element results, the data is positioned on the line $r_e = r_t$. Data distributed above the line $r_e = r_t$ indicates that the buckling curve provides conservative values for the column strength. Unconservative columns strengths are found when the data points are below $r_e = r_t$. When the buckling curve formulation represents column strengths different from those obtained with finite element analyses the data points will be distributed around the line $r_e = R_m \cdot r_t$, where R_m is mean value correction factor according to equation (13), [11, 19]. This line will give a better description of the correlation between the theoretical and numerical values in comparison to $r_e = r_t$.

The partial factor associated with the uncertainty of the resistance model is evaluated for each buckling curve. The corresponding γ_{Rd} -values for each section type and buckling axis are presented in Table 6. For unfavorable buckling curves the γ_{Rd} -value is lower in comparison to more favorable buckling curves for a majority of the investigated cases. Hence, relating the elastic-plastic buckling response of a heavy HISTAR 460 section to a more favorable buckling curve is at the expense of a higher partial factor γ_{Rd} . The most favorable buckling curve

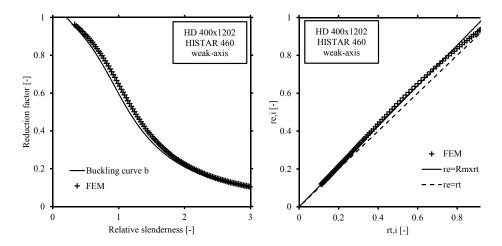


Fig. 12 - Finite element data in buckling curve (left) and compared against theoretical solutions for buckling curve b (right) - weak-axis buckling of HD 400x1202 in HISTAR 460.

selected for heavy HISTAR 460 sections failing by flexural buckling is based on the criterion $\gamma_{Rd} < 1.05$, as denoted in bold in Table 6. This is associated with a target value $\gamma_{Rd} = 1.0$ so that values greater than 1.05 cannot be accepted. The 1.05 boundary is arbitrary but it is believed to be reasonable.

The differences between sections belonging to the same type (HD or HL) and buckling around the same axis (weak or strong) are relatively small, indicating that section geometry for the same section type has little influence on the partial factor.

In general the partial factors for an identical buckling curve are greater for the weak-axis buckling case than those for the strong-axis buckling case. This reflects the more detrimental influence of residual stresses for columns failing by weak-axis buckling. Assuming that a γ_{Rd} -value smaller than 1.05 allows $\gamma_{Rd} = 1.0$ to be used, HD and HL sections failing by weak-axis buckling should be assigned to buckling curve "b". Buckling curve "a₀" is assigned to HD sections failing by strong axis buckling. HL sections buckling about the strong axis should be checked by buckling curve "a". These results are summarized in Table 7.

4.2.2 Steel grade S460

For S460 four different cross-sections were considered, namely HD 400x900, HD 400x1299, HL 920x1194 and HL 920x1377, see Table 2. For each cross-section the weak-axis and strong-axis buckling response was evaluated. The relative slenderness of the investigated columns was in the range between 0.23 and 3.33.

Table 6 - Partial factors γ_{Rd} per buckling curve for HISTAR 460

			Buckling curve				
Heavy section	Buckling	Sample	a0	a	b	c	d
Tieuvy section	axis	size n	uo	u	U	·	u
HD 400x900	Weak-	104	1.161	1.054	0.994	0.978	0.947
11D 400x300	Strong	119	1.015	1.000	0.998	0.984	0.950
HD 400x990	Weak	104	1.160	1.054	1.003	0.991	0.968
HD 400x990	Strong	111	1.016	1.010	1.017	1.015	0.995
HD 400x1086	Weak	109	1.159	1.053	1.000	0.989	0.964
HD 400x1080	Strong	109	1.015	1.012	1.022	1.021	1.004
HD 400x1202	Weak	110	1.160	1.053	0.997	0.983	0.955
HD 400X1202	Strong	134	1.016	1.009	1.017	1.013	0.992
HD 400x1299	Weak	110	1.160	1.053	0.999	0.985	0.957
HD 400X1299	Strong	137	1.017	1.009	1.011	1.003	0.978
HL 920x1377	Weak	100	1.275	1.146	1.017	0.982	0.953
HL 920X13//	Strong	166	1.053	0.992	0.983	0.964	0.922
HL 920x1194	Weak	101	1.298	1.167	1.031	0.974	0.933
ПL 920X1194	Strong	106	1.073	0.991	0.967	0.940	0.887
HL 920x1269	Weak	103	1.287	1.158	1.030	0.985	0.953
ПL 920X1209	Strong	101	1.056	0.993	0.985	0.969	0.931

Table 7 - Proposed buckling curves for HISTAR 460 sections based on γ_{Rd}

Cross-section	Limits	Buckling	Buckling
		about axis	curve
Rolled I-sections			
Z			
	HD section:	у-у	a_0
t_{f} \uparrow	$h/b \approx 1.23$	Z-Z	b
$\frac{1}{2}$			
у у	HL section:	у-у	a
	$h/b \approx 2.35$	Z-Z	b
$ \leftarrow b $			

Figure 13 (left) shows the finite elements results for a HL 920x1377 section in S460 buckling about its strong axis in a buckling curve diagram in addition to buckling curve "a". In Figure 13 (right) the same results are plotted with the theoretical column strength $r_{\rm t,i} = \chi$ on the horizontal axis against its numerical counterpart $r_{\rm e,i} = \chi_{\rm FEM}$ on the vertical axis.

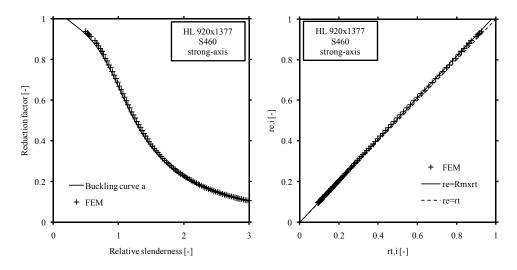


Fig. 13 - Finite element data in buckling curve (left) and compared against theoretical solutions for buckling curve b (right) – strong-axis buckling of HL 920x1377 in S460

The partial factor associated with the uncertainty of the resistance model is evaluated for each buckling curve. The corresponding γ_{Rd} -values for each section type and buckling axis are presented in Table 8. Again the partial factor should be smaller than 1.05 to allow γ_{Rd} = 1.0 to be used. The associated values are denoted in bold in Table 8.

Again the differences between sections belonging to the same type (HD or HL) and buckling around the same axis (weak or strong) are relatively small and the partial factors for an identical buckling curve are greater for the weak-axis buckling case than those for the strong-axis buckling case.

The proposed buckling curves for S460 sections are the same as for HISTAR 460 (Table 7) except for HL sections buckling around the weak axis where buckling curve "c" seems to be more appropriate. However, it should be noted that for that case the partial factors belonging to buckling curve "b" ($\gamma_{Rd} = 1.066$ and $\gamma_{Rd} = 1.058$ for the sections HL 920x1194 and HL 920x1377, respectively) just slightly exceed $\gamma_{Rd} = 1.05$.

					Buckling	curve	
Heavy section	Buckling axis	Sample size <i>n</i>	a_0	a	b	С	d
HD 400x900	Weak	116	1.209	1.092	1.004	0.982	0.952
HD 400X900	Strong	106	1.033	1.002	1.009	1.005	0.983
HD 400x1299	Weak	131	1.208	1.091	1.005	0.980	0.945
HD 400X1299	Strong	105	1.035	1.003	1.008	1.002	0.978
HL 920x1194	Weak	100	1.356	1.218	1.066	0.978	0.935
ПL 920X1194	Strong	115	1.101	0.999	0.963	0.934	0.880
HL 920x1377	Weak	108	1.355	1.214	1.058	0.990	0.972
	Strong	102	1.084	0.995	0.988	0.975	0.939

Table 8 - Partial factors γ_{Rd} per buckling curve for S460

4.2.3 Steel grades S355 and S235

Since HL cross-sections apparently result in less favorable buckling curves than HD cross-sections, only HL cross-sections were considered for 355 and S235. For two cross-sections in S355 and S235 strong-axis buckling was considered: HL 920x1377 and HL 920x1194, see Table 2. For cross-section HL 920x1377 made from steel grade S355 buckling about the weak-axis was considered. The relative slenderness of the investigated columns was in the range between 0.21 and 3.58.

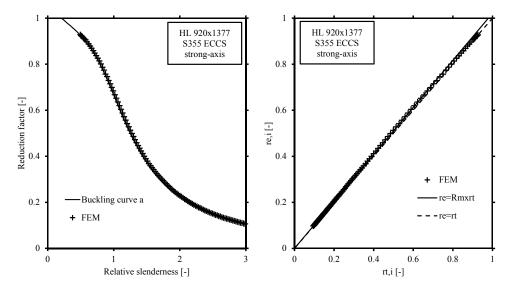


Fig. 14 - Finite element data in buckling curve (left) and compared against theoretical solutions for buckling curve b (right) – strong-axis buckling of HL 920x1377 in S355 with ECCS residual stress

Figure 14 (left) shows the finite elements results for a HL 920x1377 section in S355 with ECCS residual stress model, buckling about its strong axis in a buckling curve diagram in addition to buckling curve "a". In Figure 14 (right) the same results are plotted with the theoretical column strength $r_{t,i} = \chi$ on the horizontal axis against its numerical counterpart $r_{e,i} = \chi_{FEM}$ on the vertical axis.

The partial factors associated with the uncertainty of the resistance model are evaluated for each buckling curve and shown in Table 9. Also the residual stress model used is indicated. Again the partial factor should be smaller than 1.05 to allow $\gamma_{Rd} = 1.0$ to be used. The associated values are denoted in bold in Table 9.

For S355 and S235 table 9 suggests buckling curve "a" for strong-axis buckling and buckling curve "c" for weak-axis buckling. It should be noted that the strong-axis partial factors associated with buckling curve "a" obtained with residual stress model QST are quite close to the 1.05 boundary value. It should also be noted that no knowledge is available with respect to the real residual stress models and levels for these heavy sections in S355 and S235.

					Buckling curve					
Heavy section	Steel gr.	Res. str. mod.	Buckl. axis	Sample size <i>n</i>	a_0	a	b	с	d	
	S235	ECCS	Strong	115	1.122	1.026	1.016	1.018	1.008	
HL	S355	ECCS	Strong	120	1.093	1.002	0.985	0.972	0.937	
920x1377		S355	355 QST	Strong	115	1.151	1.037	0.995	0.983	0.949
		QS1	Weak	120	1.502	1.347	1.170	1.029	0.964	
HL 920x1194	S235	ECCS	Strong	142	1.129	1.029	1.021	1.008	0.990	
		ECCS	Strong	123	1.095	1.014	1.005	1.001	0.983	
		8355	QST	Strong	122	1.160	1.044	0.994	0.986	0.958

Table 9 - Partial factors γ_{Rd} per buckling curve for S355 and S235

4.3 Statistical information on materials

The presented analyses so far were limited to the computation of γ_{Rd} -values. Using available statistical information on the partial factor for the material γ_m and using equation (2) may produce lower γ_{M1} -values than the γ_{Rd} -values, since γ_m -values are generally smaller than 1.0. The relevant material property is the yield stress. So, if statistical information on the yield stress is available such that a γ_m -value can be evaluated, then the general partial factor γ_{M1} can be calculated with equation (2). As the yield stress of a single coupon can never be lower than the nominal yield stress, as this would lead to the member being rejected, it can be reasonably assumed that a γ_m -value of 1.0 is a conservative value to account for the variability of the material properties. So, if statistical information on the yield

stress is not available, the partial factor for the material γ_m can be safely set equal to $\gamma_m = 1.0$ and the general partial factor – based on equation (2) – is equal to $\gamma_{M1} = \gamma_{Rd}$.

4.3.1 Steel HISTAR 460

Since for HISTAR 460 published statistical information on the yield stress is not yet available $\gamma_{\rm m}=1.0$ is used to compute the general partial factor $\gamma_{\rm M1}$ according to equation (2): i.e. $\gamma_{\rm M1}=\gamma_{\rm Rd}$. Assuming that $\gamma_{\rm M1}=1.0$ is the target value for the general partial factor, then the (arbitrary but reasonable) criterion for choosing a buckling curve is that $\gamma_{\rm M1}<1.05$. So, in fact for HISTAR 460 with $\gamma_{\rm M1}=\gamma_{\rm Rd}$, also the partial factor should fulfil the requirement $\gamma_{\rm Rd}<1.05$. This means that for HISTAR 460 the buckling curves of Table 7 can be used with $\gamma_{\rm M1}=1.0$. As soon as a database becomes available containing the yield stress from a wide set of coupon tests on HISTAR 460 sections, a value of $\gamma_{\rm m}$ lower than 1.0 can be obtained resulting in either a lower general partial factor or a more favorable buckling curve.

4.3.2 Steel grade S460

For S460, statistical literature information concerning the yield stress f_y , is used to estimate $\gamma_m < 1.0$. Two RFCS (Research Fund for Coal and Steel) projects provide statistical data: OPUS [20] and PROQUA [21].

OPUS [20] provides statistical data for the yield stress of S460M in the flange thickness range of $16 < t_f < 40$ mm: the mean value is $f_{y,m} = 521.1 \text{ N/mm}^2$, the standard deviation is $f_{y,\sigma} = 26.75 \text{ N/mm}^2$ and the coefficient of variation then is $V_{fy} = f_{y,m}/f_{y,\sigma} = 0.051$. The ratio between mean and nominal yield stress can be calculated as $R = f_{y,m}/f_{y,nom} = 521.1/460 = 1.13$. If it is assumed that this ratio also applies to S460 cross-sections with flange thicknesses $t_f > 100$ mm, then with a reduced nominal yield stress for thickness $f_{y,nom} = 385 \text{ N/mm}^2$, the mean value becomes: $f_{y,m} = f_{y,nom} R = 385 \cdot 1.13 = 435 \text{ N/mm}^2$. Keeping the coefficient of variation the same, the material partial factor can be calculated using:

$$\gamma_{\rm m} = \frac{f_{\rm y,nom}}{f_{\rm y,m} (1 - 1.64 V_{fy})}$$
 (20)

This results in $\gamma_m = 385/(435(1-1.64 \cdot 0.051)) = 0.966$. If this material partial factor is used with the partial factors γ_{Rd} of Table 8 in equation (2), more favorable general partial factors γ_{M1} are obtained. This does not affect the buckling curves for HD sections nor does it affect the buckling curve for strong-axis buckling of HL columns but it does affect the buckling curve for weak-axis buckling of HL columns. For HL columns in weak-axis buckling and for buckling curve "b" the γ_{Rd} -values are 1.066 and 1.058 for HL 920x1194 and HL 920x1377 respectively.

Multiplied (equation (2)) by $\gamma_{\rm m} = 0.966$ the $\gamma_{\rm MI}$ -values become 1.030 and 1.022 respectively. So $\gamma_{\rm MI} < 1.05$ meaning that $\gamma_{\rm MI} = 1.0$ may be used in this case together with buckling curve "b". This means that also for S460 the buckling curves of Table 7 can be used with $\gamma_{\rm MI} = 1.0$.

Statistical data given in PROQUA [21] together with plant measurements support the value $\gamma_m = 0.966$ used.

4.3.3 Steel grades S355 and S235

Though statistical information on the yield stress of S355 and S235 is readily available, there are other reasons (to be mentioned hereafter) not to use this information.

5. BUCKLING CURVES FOR EUROCODE3

Though for HISTAR 460 and S460 the buckling curves of Table 7 may be used for heavy sections with h/b > 1.2 and $t_f > 100$ mm in combination with the general partial factor $\gamma_{\rm MI} = 1.0$, these buckling curves cannot be incorporated in Eurocode3 EN 1993-1-1 [8] if the format of the buckling curve selection table (see Table 1) is to be kept, since no distinction is made between HD and HL cross-sections. For that reason, the most unfavorable buckling curves for HD and HL cross-sections of Table 7 are used in the proposed new Eurocode3 buckling curve selection table (Table 10). Also the proprietary name HISTAR can obviously not be mentioned in the proposed Eurocode3 buckling curve selection table.

For S355 and S235 it was shown in section 4.2.3 that for heavy sections with h/b > 1.2 and $t_f > 100$ mm the buckling curves "a" and "c" may be used for strong and weak-axis buckling respectively, together with $\gamma_{Rd} = 1.0$. This result may even be improved using statistical data on the yield stress resulting in $\gamma_{m} < 1.0$ and thus in either a lower value of the general partial factor γ_{M1} or in more favorable buckling curves than mentioned. However, this does not make sense as long as no further and better information is available on residual stress distributions in heavy sections with h/b > 1.2 and $t_f > 100$ mm in S355 and S235. In fact, information on residual stresses is not available at this moment at all. For that reason it is proposed to conservatively use the buckling curves "b" and "c", which fit nicely in the table when comparing with buckling curves for other cases. Often, moving from S460 to lower steel grades means a shift of one buckling curve and the current proposal is in line with that.

The QST residual stress model [9] as used in the present analyses is representative for any heavy wide flange section having similar cross-sectional dimensions and made with the Quenched and Self-Tempered process. As such, the

residual stress model can be used to define the initial stress state in heavy sections made from grade S460 but also from S500 as these grades are manufactured with identical methods by ArcelorMittal as HISTAR 460 steel. Grade S500 also has the same nominal yield stress after reduction to account for material thickness effects (i.e. 450 N/mm², see Figure 1). For these reasons S500 can be added in the last column of Table 10.

			Buckling	Bucklin	g curve
			about	S235	S460
Cross-section		Limits	axis	S275	S500
				S355	
				S420	
Rolled I-sections			77.77	0	0
		$t_{\rm f} \leq 40~{\rm mm}$	у-у	a	a_0
		•	Z-Z	b	a_0
Z				1	
\ \	h/b > 1.2	$40 < t_{\rm f} \le 100 \rm mm$	у-у	b	a
$t_{\rm f}$		· · · · · · · · · · · · · · · · · · ·	Z-Z	С	a
`					
$\mid \mid_h \mid_h$		$t_f > 100 \text{ mm}$	у-у	b	a
у у "		<i>ij</i> > 100 mm	Z-Z	c	b
		4 < 100	у-у	b	a
│ └─── 		$t_{\rm f} \le 100 \; {\rm mm}$	Z-Z	c	a
	$h/b \le 1.2$				
 ∪		4 > 100	у-у	d	c
		$t_{\rm f} > 100 \ {\rm mm}$	z-z	d	c

Table 10 - Proposed buckling curve selection table for Eurocode3, EN 1993-1-1

6. CONCLUSIONS

In this paper buckling curves are proposed to check the flexural buckling resistance of heavy wide flange columns, which have a flange thickness $t_f > 100$ mm and a height-to-width ratio h/b > 1.2. These sections are currently not covered by Eurocode3 (EN 1993-1-1).

A database was created containing the elastic-plastic buckling resistance for a wide set of heavy HISTAR 460, S460, S355 and S235 columns (both the stocky HD-type and slender HL-type) failing by weak-axis and strong-axis buckling. The buckling resistance was evaluated using non-linear finite element analyses using an earlier proposed residual stress model [9] and the ECCS residual stress model [10] to define the initial stress state.

The numerical buckling loads were compared against theoretical values, where the latter correspond to the buckling resistances for a selected buckling curve according to EN 1993-1-1. Based on the ratio between both values, a partial factor γ_{Rd} associated with the uncertainty of the resistance model was evaluated according to Annex D of EN 1990-1-1 for each of the five buckling curves.

Aiming at a target value for the general partial factor of $\gamma_{\rm MI} = 1.0$, meaning that the resulting $\gamma_{\rm MI}$ -values should not exceed 1.05, buckling curves are proposed. For cross-sections with h/b > 1.2 and $t_{\rm f} > 100$ mm in steel grades S460 and S500 the buckling curves "a" and "b" are proposed for strong and weak-axis buckling respectively, while for these cross-sections in steel grades S235 up to and including S420 the buckling curves "b" and "c" are proposed for strong and weak-axis buckling respectively.

Quenched and Self-Tempered (QST) steel cross-sections are currently manufactured under the proprietary name HISTAR (HIgh STrength ARcelorMittal) by ArcelorMittal. For stocky HD cross-sections in HISTAR 460 with $h/b \approx 1.23$ and $t_{\rm f} > 100$ mm it was shown that the buckling curves "a₀" and "b" can be used for strong and weak-axis buckling respectively. For slender HL cross-sections in HISTAR 460 with $h/b \approx 2.35$ and $t_{\rm f} > 100$ mm it was shown that the buckling curves "a" and "b" can be used for strong and weak-axis buckling respectively.

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